

2 **Towards a unified model of pavlovian conditioning: short review**
3 **of trace conditioning models**

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7 **Abstract** There are three basic paradigms of classical
8 conditioning: delay, trace and context conditioning where
9 presentation of a conditioned stimulus (CS) or a context
10 typically predicts an unconditioned stimulus (US). In delay
11 conditioning CS and US normally coterminate, whereas in
12 trace conditioning an interval of time exists between CS
13 termination and US onset. The modeling of trace condi-
14 tioning is a rather difficult computational problem and is a
15 challenge to the behavior and connectionist approaches
16 mainly due to a time gap between CS and US. To account
17 for trace conditioning, Pavlov (Conditioned reflexes: an
18 investigation of the physiological activity of the cerebral
19 cortex, Oxford University Press, London, 1927) postulated
20 the existence of a stimulus “trace” in the nervous system.
21 Meanwhile, there exist many other options for solving this
22 association problem. There are several excellent reviews of
23 computational models of classical conditioning but none
24 has thus far been devoted to trace conditioning. Eight
25 representative models of trace conditioning aimed at
26 building a prospective model are being reviewed below in a
27 brief form. As a result, one of them, comprising the most
28 important features of its predecessors, can be suggested as
29 a real candidate for a unified model of trace conditioning.
30

31 **Keywords** Attention · Trace conditioning ·
32 Septo-hippocampal system · Unified model

Variety of the computation mechanisms of trace conditioning 33
34

Theoretical preview 35

There are four basic paradigms of the classical condition- 36
ing (see Fig. 1) where presentation of a conditioned stim- 37
ulus (CS) or context typically predicts an aversive outcome 38
such as a shock. A conditioned response (CR) to a CS alone 39
is taken as evidence that association between the CS and 40
the unconditioned stimulus (US) has been learned. Delay 41
and trace procedures differ in the temporal relationship 42
between CS and US. In delay conditioning CS and US 43
normally coterminate, whereas in trace conditioning some 44
time passes between a CS termination and an US onset. 45
The delay conditioning is usually not hippocampus- 46
dependent, while trace and context conditioning typically 47
result in a weaker response than delay conditioning does 48
and require an intact hippocampus. The magnitude of trace 49
conditioning is inversely related to the duration of the trace 50
interval. 51

Modeling of trace conditioning is a rather difficult 52
computational problem mainly due to a time gap between 53
CS and US. To account for trace conditioning, Pavlov 54
(1927) postulated the existence of a stimulus “trace” in the 55
nervous system which did not disappear with the physical 56
stimulus, but persisted long enough to allow associations 57
between this trace and a subsequent US even in the case of 58
a time gap between CS and US presentations. Meanwhile, 59
there exist many other ways to solve the association 60
problem. For example, some researchers suggested restor- 61
ing the contiguity between CS and US by means of a 62
tapped delay-line (Desmond and Moore 1991; Zipsler 1986) 63
or by stochastic sustained neural activity (Yamazaki and 64
Tanaka 2005; Rodriguez and Levy 2001), or by using an 65

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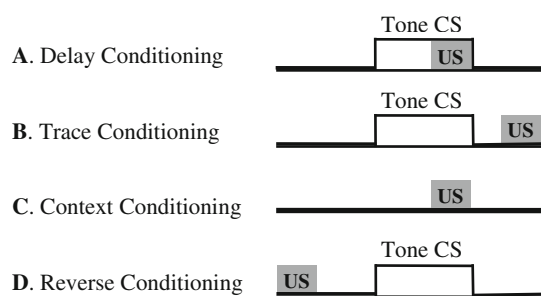


Fig. 1 Four basic paradigms of classical conditioning

66 STM to fill the time gap (Larrauri and Schmajuk 2008).
 67 These approaches allowed explanation of many new data
 68 and put restrictions on a possible neuronal mechanism of
 69 trace conditioning. It will be useful to have a closer look at
 70 such approaches which may provide components for a
 71 unified model of trace conditioning.

72 According to Marchand et al. (2004), there are basically
 73 three classes of theoretical descriptions of trace condi-
 74 tioning: timing models, multiple-time-scale models and
 75 conditioning of secondary cues. Each is briefly described as
 76 follows. According to the timing models, any association is
 77 indicative of the of time interval between the events,
 78 wherefore trace conditioning is not different in nature from
 79 simple delay conditioning. A trace interval does not pre-
 80 vent establishment of an association, because it is the time
 81 that is encoded rather than the residual trace of a particular
 82 stimulus. According to the multiple-time-scale models, any
 83 sensory event elicits multiple parallel basis functions in the
 84 central nervous system, each function having its particular
 85 time course. Basis functions may be triggered by the CS
 86 onset or offset, but will not necessarily be maintained
 87 during the CS. Thus, the time elapsed since the event is
 88 uniquely represented by a pattern of active basis functions,
 89 and this pattern can become associated with the US. The
 90 third way to account for trace conditioning is to assume
 91 that CS somehow becomes associated with other stimuli
 92 that call up secondary cues which can bridge the temporal
 93 gap between CS and US. According to this theory, each
 94 stimulus, context including, is composed of a set of ele-
 95 ments which become associated together as long as they
 96 are simultaneously presented. Trace fear conditioning
 97 should first generate CRs to both the context and the CS
 98 trace. Contextual conditioning is often parallel to long-
 99 trace fear conditioning, it is sensitive to hippocampal
 100 lesions and can bridge the time gap. One can also include
 101 in this list the traditional, and recently updated, attentional
 102 theory of trace conditioning. According to the present-day
 103 attentional theory, increases and decreases in attention can
 104 influence the stimulus processing response in such a way
 105 that the time gap between CS and US will be bridged by

additional attentional resources governed by novelty 106
 (Larrauri and Schmajuk 2008). 107

Besides the timing problem, the main question is what 108
 function of the hippocampus is necessary during trace and 109
 contextual conditioning, but is not needed in delay condi- 110
 tioning. There have been proposed several theories regarding 111
 the specific role of the hippocampus during trace condi- 112
 tioning. For example, the hippocampus may be needed to 113
 overcome stimulus discontiguity (Wallenstein et al. 1998), to 114
 time CRs accurately (e.g. Balsam et al. 2002) or to distin- 115
 guish between the intertrial interval and the trace interval 116
 (Bolles et al. 1978). Another possibility is that the hippo- 117
 campus is more active during complicated and difficult 118
 forms of classical conditioning (Beylin et al. 2001; Quinn 119
 et al. 2008; Shors 2004). Trace conditioning, according to 120
 Clark et al. (2001), is fundamentally different from delay 121
 conditioning. It resembles delay conditioning in that it also 122
 depends on the cerebellum (Takehara et al. 2003; Clark and 123
 Squire 2004) but it is additionally dependent on the hippo- 124
 campus and the neocortex (for a review see Clark et al. 2002). 125
 Another theory is that it is trace but not delay conditioning 126
 that is an associative learning task dependent on awareness 127
 which requires hippocampus activity (Clark and Squire 128
 1998, 2004; Cheng et al. 2008; Shors 2004). 129

There are several excellent reviews of computational 130
 models of classical conditioning (e.g. Vogel et al. 2004; 131
 Schmajuk 2008; Moustafa et al. 2009) that have provided 132
 mathematical and/or simulation explanation and described 133
 of various effects of delay conditioning in the last 40 years. 134
 Below, we shall briefly review some representative models 135
 of trace conditioning with the aim of establishing a pro- 136
 spective unified model. For each model we follow the same 137
 outline: the class of the model, the main task of the model, 138
 the model architecture, the learning rule, the main predic- 139
 tions, possible specific contributions to the unified model, 140
 as well as its limitations. 141

The tapped delay-lines model (Desmond and Moore 142
 1991) 143

This model belongs to the multiple-time-scale class of 144
 models. It was developed from earlier neuronal network 145
 models of trace conditioning proposed at first to associate 146
 noncontiguous stimuli by means of a delay line to a delay 147
 CS until a US comes. It allows simulating the following 148
 complex timing characteristics of CRs: (1) in trials pre- 149
 senting a CS alone, the CR would reach its maximum at the 150
 time a US would be expected; (2) CR onset tends to be 151
 delayed for a period corresponding to the expected time of 152
 the US; (3) the length of the delay of the CR depends upon 153
 the CS–US interstimulus interval (ISI), but the CR timing 154
 is also adaptive in that a change in the ISI produces a 155
 corresponding change in the time of the peak; (4) double 156

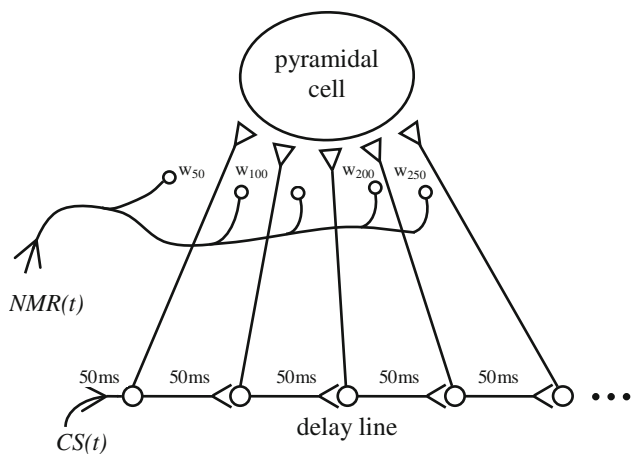





Fig. 2 Basic structure of the hippocampal delay line model of adaptive timing as proposed by Zipser (1986). Each synapse  introduces a delay; the total delay from activation of the first element in the delay-line to the last element is a direct function of the number of sequential synapses. Taps from the delay-line units send timing information to higher-order processing units. $NMR(t)$ is the nictitating membrane response produced by US, which acts as teaching signal.  unmodified,  modified synapse. CS input initiates sequential propagation of signal through a *delay-line*

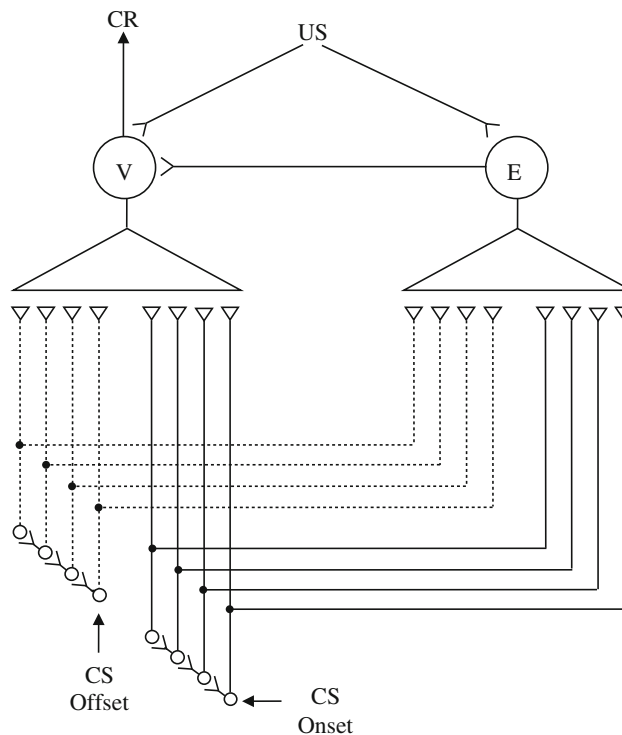



Fig. 3 Diagram of the tapped delay-line network (from Desmond and Moore 1991). CS onset and CS offset are assumed to activate separate tapped *delay-line* stimulus traces. The taps form modifiable connections—denoted by closed () synaptic terminals—with the V and E units. CR is generated when V-unit connections that have positive weights are activated

157 peaks are also observed if the ISI alternates between two
158 different values.

159 The original idea (due to Zipser 1986) of using the
160 tapped delay-line to compensate the variable trace interval
161 in the nictitating membrane response (NMR) is illustrated
162 in Fig. 2. If the output from all these taps is used as the CS
163 input to the hippocampus, then pulses of the CS-derived
164 signal will overlap all phases of the undelayed NMR. It is
165 only those synapses emanating from the taps at the
166 appropriate delays that will be strengthened, because they
167 will be the only ones where CS and NMR activities are
168 coincident in time. Thus, this network describes in principle
169 the ability to learn both the ISI and the time–amplitude
170 profile of the NMR. The full network architecture is
171 illustrated in Fig. 3. Basically, each CS is committed to
172 activate two tapped delay-lines: one at the onset of the CS
173 and the other at the offset. Each tap forms Hebb-like
174 modifiable connections¹ with two units, labelled V and E.

1FL01 ¹ In classical conditioning, it is often assumed that presynaptic inputs
1FL02 from CSs and US converge on one or more postsynaptic units. The
1FL03 postsynaptic unit initially responds strongly to the US input, but only
1FL04 weakly to the CS input. Through repeated CS–US pairings, the
1FL05 connection strength of the CS input is altered so that the CS becomes
1FL06 capable of eliciting a robust output from the postsynaptic unit.
1FL07 Alternatively, both CS and US can converge presynaptically, thus
1FL08 performing non-Hebbian learning as in Zipser (1986). However, both
1FL09 the Hebbian and non-Hebbian learning rules are problematic for trace
1FL10 conditioning in view of the unsolved problem of shifting information
1FL11 from the hippocampus to the cortex (see Frey and Morris 1997;
1FL12 Lesburguères et al. 2011).

The function of the E-unit is to learn the time of US
175 occurrence relative to the onset and offset of all CSs, which
176 corresponds to the tap with the strongest connection. With
177 repeated CS–US presentations, the E-unit starts sending a
178 signal to the V-unit indicating the time when a US is
179 expected. This signal permits the V-unit connection
180 strengths to be modified. The network’s output (the simulated
181 CR) is derived from the V-unit. As each tap is activated,
182 its connection weight contributes to the magnitude
183 of the CR, affecting it in either an excitatory (positive
184 weight) or inhibitory (negative weight) manner, thus simulat-
185 ing the above CR complex. This model makes a prediction
186 that an increase of the CS duration will produce
187 double-peaked CRs. Indeed, CR peaks were often observed
188 at two different points at a time when the duration of a
189 trace-conditioned CS was lengthened.

190 While some investigators observed that the arrangement
191 of parallel fibers in the cerebellar cortex resembled a delay-
192 line, Moore et al. (1989) suggested that the timing func-
193 tions were performed by the cerebellum, and according to
194 Zipser (1986), the tapped delay-line input to hippocampal
195 neurons could account for the response firing properties of
196 those neurons during rabbit NMR conditioning. Whether
197

198 the tapped delay-line stimulus processing is a neurobio-
199 logically plausible mechanism, especially with long delays
200 (tens of seconds) or is simply an analogy for the timing
201 processes that underlie conditioning, is an open question.
202 The timing mechanism assumed in this model is specula-
203 tive. Although the tapped delay-line structure is capable of
204 providing the timing functions necessary for CR appear-
205 ance, it cannot account for the ISI function, which is the
206 conditioning strength plotted as a function of the CS-US
207 interval, which tends to have an inverted-U shape.

208 Nevertheless, the use of the delay-line in stimulus pro-
209 cessing is supported by single-neuron studies of the limbic
210 system (Vinogradova 2001; McEchron et al. 2003;
211 Gilmartin and McEchron 2005) although the role of CS
212 offset is relatively insignificant (Burman and Gewirtz
213 2004). The tapped delay-line is probably an indispensable
214 part of the mechanism of trace conditioning and should be
215 utilized in the unified mechanism of trace conditioning, if it
216 is physiologically supported.

217 The temporal basis functions model (Ludvig et al.
218 2008)

219 This model also belongs to the multiple-time-scale class of
220 models of trace conditioning and is designed to solve more
221 complicated problems. It is a reinforcement-learning con-
222 nectionist model describing the role of the hippocampus in
223 classical conditioning, focusing on the difference between
224 the trace and delay conditioning. It is a modern variety of
225 the so-called spectral models that perform Fourier-like
226 stimulus representation. In particular, all stimuli are rep-
227 resented both as an intact whole and as a series of temporal
228 elements with varying delays. These two stimulus repre-
229 sentations interact, producing different patterns of learning
230 in the trace and delay conditioning.

231 The model consists of three separate modules: the
232 stimulus representation, the learning algorithm, and the
233 response rule. The stimuli are represented as a series of
234 basic elements or internal microstimuli, which are gradu-
235 ally broadening elements of Gaussians. The model learns
236 through a well-known Sutton-Barto algorithm (Sutton and
237 Barto 1998), which can be explained as follows. At each
238 time step, the US prediction is determined by the linear
239 weighted combination of the above basis functions. This
240 US prediction is compared to the reward received in the
241 comparator to generate a time difference error which is
242 then used to update the weight vector. Finally, these US
243 predictions are used as a driving into responses through a
244 simple, threshold leaky-integrator response rule.

245 The model suggests that hippocampal lesions eliminate
246 the long-latency temporal elements, but preserve the short-
247 latency ones. In accord with the empirical data, simulated
248 hippocampal damage impairs trace conditioning, but does

not delay conditioning at medium-length intervals. With
249 the longer intervals, learning is impaired in both proce-
250 dures, with shorter intervals in neither. As it is mentioned
251 in the *Theoretical preview*, there are several theories for the
252 role of the hippocampus in trace conditioning, including
253 modulation of timing, establishment of contiguity, and
254 overcoming of task difficulty. This model is designed to
255 provide a computational mechanism that could unite these
256 three proposed theories.
257

258 Although a simple Gaussian basis function approach
259 suffices for the datasets considered in the connectionist
260 approach, other related mathematical functions are certainly
261 possible. For example, replacing the temporal microstimuli
262 in this model with the spectral traces as in Grossberg and
263 Schmajuk (1989) produces results that are similar to this
264 model. However, there is one important characteristic of the
265 microstimulus series in both cases which shows that the
266 individual elements should not decay too quickly. Another
267 key challenge for the future modeling is reconciling the
268 abstract account of the hippocampal function in trace con-
269 ditioning of this model with the approaches that consider
270 some greater physiological details (e.g. Rodriguez and Levy
271 2001; Yamazaki and Tanaka 2005, see later). At the same
272 time, the principle of comparator and the feedback learning
273 by extracting the time difference error is essential for the
274 unified model of trace conditioning.

Inherent dynamics model (Rivest et al. 2009) 275

276 The representation gained by this model can be viewed as
277 learning one of the temporal basis functions and associating it
278 with a relevant stimulus, while the previous two models need
279 to be given a whole set of fixed basis functions, covering the
280 necessary temporal space for every possible stimulus. Delay-
281 line representations require multiple predefined lines with
282 specific parameters to accommodate all the possible timing
283 information for all possible stimuli of a given task, similar to
284 having axons of various lengths or diameters or a set of
285 polysynaptic connections. This seems physiologically unre-
286 alistic for delays in the order of seconds. The proposed model
287 involves a representation of the environment dynamics in an
288 adaptive biologically plausible framework, and predicts a US
289 without a recourse to delay lines or other special-purpose
290 timing circuits. The model predicts that the task-dependent
291 representation of time is learned by experience, is encoded in
292 ramp-like changes in a single-neuron cortical activity dis-
293 tributed across small neural networks, and points out a tem-
294 poral integration mechanism resulting from the inherent
295 dynamics of recurrent connections within the network. The
296 model also reproduces the known finding that trace condi-
297 tioning is more difficult than delay conditioning.

298 The major weakness of this model at the moment is the
299 considerable extent of training it requires using a method

300 similar to back propagation. In the best cases, some net-
 301 works learned the task in about 4,000 trials. The model
 302 clearly cannot accommodate the rapid acquisition of timing
 303 found in animals (e.g. Balsam et al. 2002). Animals are
 304 probably helped by an episodic memory system such as the
 305 hippocampus, while a lack of episodic memory in this
 306 model could also be a crucial factor contributing to a slow
 307 learning rate and a limited insight in this model. Acquisi-
 308 tion of an eye-blink trace conditioning without the hippo-
 309 campus is very difficult, sometimes almost impossible even
 310 with 1- or 2-s delays, although with shorter delays it may
 311 well take place within the neocortex-cerebellum network.
 312 This model can direct trace modeling to neocortical col-
 313 umns as a possible place of long STM traces in trace
 314 conditioning (cf. Larrauri and Schmajuk 2008) if the
 315 extension to long delays is possible, e.g. by slowing down
 316 cortical column intrinsic dynamics near the point of phase
 317 transitions, as described in the following model.

318 Phase transition model (Rodriguez and Levy 2001;
 319 Levy et al. 2005a, b)

320 This model, like the previous one, stresses the importance of
 321 the inherent dynamics of neuronal activity not in the neo-
 322 cortex but in the hippocampus which is able to effectively
 323 bridge the time gap by means of activity that emerges upon
 324 an increase of synaptic connection strengths as a result of
 325 learning and subsequent phase transition. The model
 326 hypothesizes the hippocampus functions as a time-indexed
 327 encoding device for the CS, rather than as a CS storage
 328 buffer. Specifically, the CS initiates a sequence of neural
 329 activity during the trace interval which is but indirectly
 330 representative of the CS. This sequence of CS-initiated firing
 331 patterns is stable enough across training so that neurons that
 332 are consistently active at the end of the interval become
 333 associated with the US. But initially, the CS-initiated activity
 334 is low and only after some training does it become self-
 335 sustained to the point of bridging the time gap between CS
 336 and US. This basic result is robust to variations in input size,
 337 length, and adjustments to parameters.

338 The model may be outlined as follows: neurons are
 339 McCulloch-Pitts-type threshold elements; input is a weigh-
 340 ted sum; output is a binary threshold of this sum with no
 341 memory of the past. Recurrent excitatory connections are
 342 sparse and randomly distributed. Inhibitory neurons control
 343 activity in a broad manner. Most connections are excitatory,
 344 have a time-spanning, and can be modified associatively
 345 based on a local Hebbian-type rule.

346 The model allows making two predictions: Some cells
 347 will increase their activity only during the trace interval,
 348 and some US-coding cells will shift in time and fire before
 349 US onset. That is, some US-related neurons will be acti-
 350 vated earlier in time, during a trial before the initial

351 increase in CRs. These neurons are responsible for pre-
 352 dictive US encoding in the hippocampus which provides
 353 information for timing an anticipatory CR.

354 The model presents the hippocampus as the critical site
 355 of US prediction in the brain mainly due to the state of
 356 phase transition in the CA3 field. The boundary line of its
 357 phase diagram shows the upper boundary of the reliably
 358 learnable trace interval. During this transition, three
 359 behaviorally distinguishable modes of eye-blink condi-
 360 tioning can occur: failure to blink; blinking too soon; and
 361 occasionally, appropriate predictive blinking.

362 The authors believe these simulations to provide cur-
 363 rently the best explanation of how the hippocampus can
 364 predict a US across a learnable trace interval by using
 365 dentate gyrus with CA3 as a recoder and CA1-subiculum
 366 with deep layers of entorhinal cortex as a decoder. However,
 367 the network of formal neurons used in the model does not
 368 necessarily predict the phase transition in more realistic
 369 neuronal nets due to the exponential decay of membrane
 370 potential and stochastic spike activity (Kryukov 2008).
 371 Besides, stochastic activity in the hippocampus alone cannot
 372 explain the complex timing characteristics of CRs, as
 373 described by the tapped delay-lines model. Therefore, some
 374 important operations for US prediction must be performed
 375 beyond the hippocampus as can be seen in the models
 376 described below.

377 The strength of this model lies in the fact that trace
 378 conditioning is considered not as attributed to the single
 379 neuron activity, but as an emergent phase transition prop-
 380 erty in the stochastic net activity of the whole hippocam-
 381 pus. Contrary to an almost universally held view, the
 382 hippocampus here is not a memory store, but performs a
 383 rather simple operation of the US timing prediction. These
 384 ideas are yet to be further developed in the unified model of
 385 trace conditioning.

386 Septo-hippocampal model (Yamazaki and Tanaka
 387 2005)

388 This model suggests using the septo-hippocampal loop to
 389 stop sustained hippocampal activity during trace condition-
 390 ing that is needed to bridge the CS-US time gap and to start a
 391 new learning cycle. For that purpose the CA3 network is
 392 modeled as having both a recurrent all-to-all excitatory and
 393 random inhibitory connections and an output neuron corre-
 394 sponding to a neuron in CA1 which is connected to all
 395 excitatory neurons in the model, with synaptic weights rep-
 396 resenting Schaffer collaterals. The study of the dynamics of a
 397 neural network that has both recurrent excitatory and random
 398 inhibitory connections shows that neurons start to become
 399 active when a relatively weak transient excitatory signal is
 400 presented, and that this activity is sustained due to the
 401 recurrent excitatory connections. The sustained activity

402 stops when a strong transient signal is presented or when
403 neurons are disinhibited through the CA1-septum pathway.

404 It is assumed in this model that the output neuron will
405 only receive a US directly through another pathway cor-
406 responding to the perforant path and the CA3 neurons will
407 only receive a CS. Activation of neurons in the perforant
408 path to CA1 does not evoke neuronal activity in CA1
409 unless neurons in CA3 are activated. That is, the CA1 field
410 serves as an AND-gate for CA3 field inputs. The CA1
411 neurons excite inhibitory neurons in the septum, and these,
412 in turn, inhibit the inhibitory neurons in CA3. As a result,
413 CA3 neurons cease to be active only after the stimulation.

414 The output neuron learns to associate the US onset with
415 the CS onset, which are separated by an off-stimulus interval
416 and can be associated due to sustained CA3 activity. The
417 synaptic modification corresponds to long-term potentiation
418 (LTP) at Shaffer collaterals induced by the conjunctive
419 stimulation of the output neuron by the US and by the signals
420 from CA3 neurons.

421 The model hypothesizes that increasing activity is
422 developed in two stages. At the first stage, a time code
423 is generated, and at the second stage increasing activity is
424 develops. Therefore, the model consists of two circuits: the
425 first circuit corresponding to CA3 generates a time passage
426 signal and at the second circuit representing CA1 shows
427 increasing activity during the delay period.

428 Despite some deviations from experiments (e.g. inhibi-
429 tory reset is gradually habituating during presentations of a
430 stimulus according to Vinogradova et al. 1998) the model
431 implies close interaction of the hippocampus with other
432 brain structures. The model can explain to some extent the
433 temporal evolution of the total hippocampal activity during
434 trace conditioning but does not present any specific pre-
435 dictions apart from the modulatory role of the septum. The
436 reason for this lies in the fact that the hippocampus and the
437 septum, while playing the central role in trace conditioning,
438 alone are not sufficient to explain timing in trace condi-
439 tioning. Timing can only be accounted for by the interac-
440 tion of many brain structures as demonstrated by the
441 following model.

442 Pacemaker-accumulator model (Buhusi and Meck
443 2005)

444 This model implies that trace conditioning is not a matter
445 of forming associations between stimuli and responses but
446 involves estimations as to when an emitted response will be
447 rewarded, and this is mainly the timing problem. From this
448 perspective, the time gap issue or the difference between
449 trace and delay conditioning is a comparatively minor
450 problem.

451 Briefly, the pacemaker-accumulator model (PAM) sug-
452 gests the processing of temporal information by four

453 synchronized modular information processing systems: the
454 clock, accumulator, memory, and decision (see Fig. 4). The
455 clock system consists of a pacemaker that regularly gener-
456 ates or emits neural ticks or pulses that are transferred (via a
457 gaiting switch) to the accumulator, which accumulates ticks/
458 pulses (neural counts) that correspond to a specific CS-US
459 time interval. The raw representation of the stimulus dura-
460 tion in the accumulator is then transferred to the short-term
461 memory, a component of the PAM memory system. The
462 contents of the short-term memory are then compared with a
463 standard in the long-term (reference) memory, the second
464 component of the PAM memory system. Finally, the deci-
465 sion level of the PAM is conceptualized to include a com-
466 parator that determines an appropriate response based on a
467 decision rule involving a comparison between the interval
468 duration present in the short-term memory and the corre-
469 sponding duration in the reference memory.

470 The model predicts that conditioned responses follow a
471 normal distribution over the ISI duration and, more
472 importantly, that the width of this response distribution is
473 proportional to the length of that interval duration. The way
474 in which the mean and standard deviation of the response
475 distribution covary implies a constant coefficient of varia-
476 tion, which is usually referred to as the scalar property, and
477 resembles Weber's law, which is reflected in most sensory
478 dimensions.

479 The first challenge is to connect PAM with more con-
480 ventional cognitive psychology, in particular where it deals
481 with context, memory and attention. Numerous studies
482 have shown that attention, picking out a stimulus from its
483 context, plays a critical role in timing behavior. Another

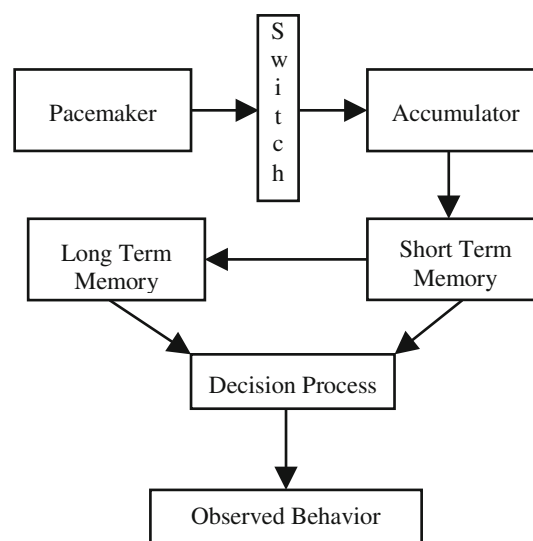


Fig. 4 Outline of the pacemaker-accumulator model. The upper level shows the pacemaker-accumulator clock, the middle level the long-term reference memory and the short-term working memory, and the lowest level the decision mechanism

484 major challenge is to understand the physiological pro-
 485 cesses underlying timing. Some researchers (e.g. Matell
 486 and Meck 2000) have criticized PAM and its derivatives on
 487 physiological grounds. The biggest drawback of PAM,
 488 however, is according to Meeter et al. (2005) that it is
 489 entirely functional, with few guidelines as to how it might
 490 be implemented in the brain. Perhaps, when it is made
 491 biologically more plausible, e.g. involving attention, and
 492 becomes closer to associative models, then both classes of
 493 models will converge to form a unified model.

494 Attentional-associative model (Schmajuk et al. 1996;
 495 Larrauri and Schmajuk 2008)

496 This is a behavior model of classical conditioning that
 497 incorporates and extends the properties of several associ-
 498 ation models to include the effects of attention, extinction
 499 and trace conditioning. Therefore, it is reasonable to con-
 500 sider it as a behavioral version of the unified model of trace
 501 conditioning. The model incorporates: (a) a mechanism
 502 capable of establishing associations between CS and US
 503 and between two CSs, (b) a real-time attentional variable
 504 regulated by the novelty of the US, the CSs, and the context
 505 (CX), and (c) a competitive rule that describes CS-US,
 506 CS-CS and CS-CX associations.

507 The model works as follows. To allow for a CS to
 508 establish associations with other CSs or a US, even when
 509 separated by a temporal gap in trace conditioning, the
 510 model suggests that the CS activates a short-term memory
 511 trace, τ_{CS} (see Fig. 5), which gradually increases over time
 512 from zero to a maximum when the CS is present and then
 513 decays back to zero when the CS is absent. It is assumed in
 514 this model that animals respond to novelty by increasing
 515 attention to environmental stimuli. The synaptic weight
 516 (represented by a triangle) connecting Node 1 to Node 2
 517 reflects the value of attention z_{CS} , which can vary between
 518 1 and -1 . When novelty is greater than a certain value,
 519 z_{CS} gradually increases; when novelty is smaller than another
 520 value, z_{CS} decreases. The novelty of a CS, CX, or US is

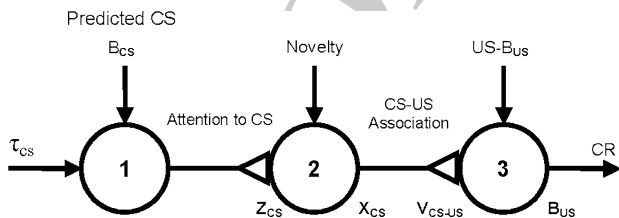


Fig. 5 A simplified diagram of the attentional-associative model (from Larrauri and Schmajuk 2008). Triangles represent variable connections between nodes. Arrows represent fixed connections between nodes. τ_{CS} —trace of the CS; z_{CS} —attention to the CS; X_{CS} —internal representation of the CS; V_{CS-US} —CS-US association; B_{CS} —predicted CS; B_{US} —predicted US; CR—conditioned response

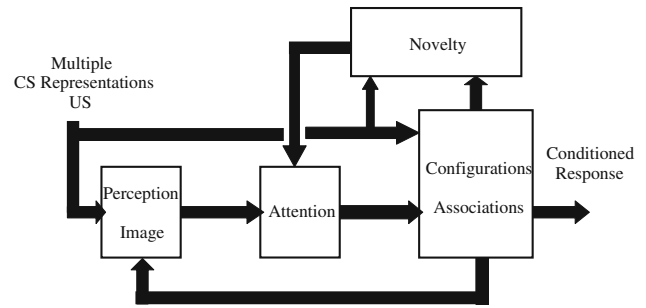


Fig. 6 A model that incorporates many of the mechanisms required to describe the multiple properties of classical conditioning (from Schmajuk et al. 1996). Novelty is the sum of the absolute values of the differences between perceived and expected (through associations with other CSs) CSs and USs. The configuration refers to internal representation of combined simple CS representations. This configural representation has the highest activity when some CSs are present and others are absent. Associations refer to the connections established between the representations of CSs and USs which allows simple and configural CSs to predict other CSs and USs

521 computed as the absolute value of the difference between
 522 the average observed value of the CS, CX, or US, and
 523 the average of the sum of all predictions for the CS, CX, or US
 524 and all active CSs and CXs. The total novelty, Novelty, is
 525 the sum of the novelties of all stimuli present or predicted
 526 at a given time, normalized between 0 and 1. Attentional
 527 control of learning (memory storage) and performance
 528 (retrieval) is the most important feature of the model.

529 Figure 6 is a block diagram of the same model which is
 530 able to describe many of the properties of classical condi-
 531 tioning, and incorporates the above mechanisms with
 532 explicit interconnections. The error correction feedback
 533 from output to input is especially important since the
 534 appearance of Rescorla and Wagner's (1972) model, and is
 535 applied here for trace conditioning to slow the CS decay in
 536 STM.

537 Common to Pavlov's theory (1927) and this model is the
 538 notion that during extinction attention to the CS decreases
 539 and this is because Novelty decreases as the prediction of
 540 the US increases. Also common to both approaches is the
 541 idea that extinction shares some properties with both
 542 habituation and latent inhibition.² In this model, both
 543 habituation and latent inhibition occur because novelty and
 544 attention to a stimulus are supposed to decrease with its
 545 repeated presentations.

546 As in the Rescorla-Wagner model, changes in associa-
 547 tions are also proportional to the difference between

² Habituation is a decrease in responsiveness to a stimulus when that stimulus is presented repeatedly or for a prolonged time. The latent inhibition refers to the effect that preexposure to a CS followed by CS-US pairings retard the generation of the CR.

Author Proof

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548 predicted and real values of the US ($US-B_{US}$). This allows
 549 explaining almost all classical effects (such as blocking,
 550 latent inhibition, etc.) as well as those requiring attention,
 551 e.g. extinction and its numerous properties. However, the
 552 model is admittedly unable to explain the important effect
 553 that extinction does not erase the original excitatory
 554 learning (e.g. Brooks and Bowker 2001), nor some other
 555 effects such as saving and overtraining (Schmajuk and
 556 Larrauri 2006).

557 Among many predictions of this model the most
 558 important is the rate of reacquisition, decreased by exten-
 559 ded extinction, which should increase with presentation of
 560 a novel CS preceding each US presentation. According to
 561 this model, the novel CS will increase Novelty, increase
 562 attention to the target CS, and speed up reacquisition. The
 563 question is: what does novelty mean in biological terms,
 564 where is it located and how is it detected in the neural
 565 system³? A more general problem of this model is that it is
 566 entirely behavior-functional and far from biological reality.
 567 No wonder that the model simulation reveals discrepancies
 568 with the relevant literature when describing the hippo-
 569 campal lesion effects on trace conditioning with shock US
 570 under short and long ISIs, and trace conditioning with an
 571 air-puff US under long ISIs. Nevertheless, this model's
 572 ability to explain many classical results when updated
 573 attentional mechanisms are incorporated is remarkable.
 574 Attention and memory should be the central aspect of the
 575 unified model of trace conditioning.

576 Theta-regulated attention model (Vinogradova 2001;
 577 Kryukov 2008)

578 This model belongs to the class of physiologically moti-
 579 vated attentional models, and therefore can in principle
 580 explain all of the abovementioned attentional effects as
 581 well as many new ones. Despite the fact that the model was
 582 originally proposed for solving of long-term memory
 583 problems, it can be easily adapted to trace conditioning as a
 584 particular case model of attention and hippocampus-
 585 dependent memory (Kryukov 2008). Indeed, here again
 586 attention is the key to all effects. It is closely connected
 587 with theta/gamma partial synchronization of basic brain
 588 structures with the specific function of binding oscillatory
 589 representations of CS, US and action, so that the CR is
 590 possible without US as a result of learning and partial
 591 synchronization. Such synchronization is most easily
 592 realized by introduction of the central oscillator with var-
 593 iable frequency acting as a global pacemaker. The sim-
 594 plified star-like architecture with a central oscillator (CO)
 595 and peripheral oscillators (POs) is given in Fig. 7. Some

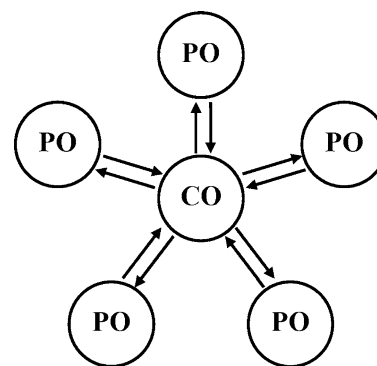


Fig. 7 Simplified architecture with central oscillator CO, and peripheral oscillators POs

POs represent a CS, some a US, and some others a final
 reaction. The association of CS and US through synchro-
 nization in trace conditioning is usually difficult because
 oscillatory CS representation decays during a trace interval.
 But repeated presentation of CS, recruiting new POs
 through phase resetting by CS and recirculating activity
 between CO and POs, leads to a stronger CS representation
 until synchronization of CS and US becomes possible
 despite the time gap. The flexible control and adaptivity are
 attributed to the forward-backward connections of POs
 with CO that can change the current frequency of ensemble
 synchronization, involving cortical, cerebellar, and amy-
 gdalar POs with different natural frequencies in various
 multimodal ensembles. Accordingly, attention is switched
 (automatically as well as voluntarily) from one group of
 oscillators to another through this changing of the fre-
 quency of the CO, thus realizing different configural and
 contextual acquisition, retrieval and extinction. Detailed
 descriptions of this model, its structure, working principles,
 and predictions are given elsewhere (Kryukov 2005, 2008;
 Kryukov et al. 1990). In this review, we shortly restate
 some details needed for understanding of the trace condi-
 tioning model.

The model works like a PLL⁴ system, well known in
 communication engineering. It comprises five standard mod-
 ules: receiver, voltage-controlled oscillator, phase detector,
 low-pass filter, and summator. Its neural representation is
 sketched in Fig. 8, based on the well-established functions of
 various parts of the limbic system (Vinogradova 2001): the

³ The answer to this question is given in biological terms by
 Vinogradova (2001) and in computational ones by Kryukov (2008)

⁴ A phase-locked loop (PLL) is an electronic control system that
 generates a signal of controlled oscillator that is locked to the phase of
 an input signal. A phase-locked loop circuit responds to both the
 frequency and the phase of the input signals, automatically raising or
 lowering the frequency of a controlled oscillator until it is matched to
 the input in both frequency and phase. For description of the PLL
 system see Gardner's text-book (1979), for application in the neuronal
 modeling based on PLL see Songnian et al. (2003) and for the
 numerical simulation of PLL with CO and several POs see
 Kazanovich et al. (1991).

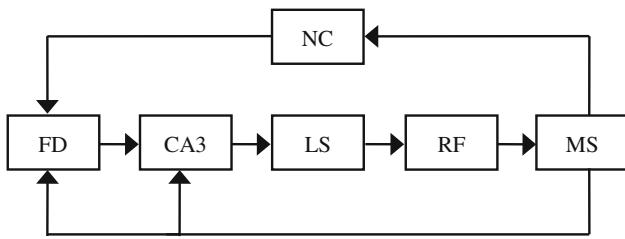


Fig. 8 Schematic diagram of the theta-regulated attention model. Abbreviations as in Fig. 9

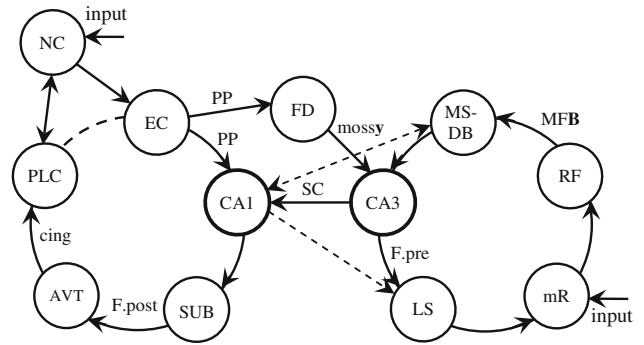


Fig. 9 Simplified scheme of two limbic circuits: regulatory and informational (adopted from Vinogradova 2001). Only principal connections are shown. AVT—antero-ventral nucleus of thalamus; CA1 and CA3—hippocampal fields; cing—cingulum; FD—fascia dentata; F.pre—fornix precommissuralis; F.post—fornix postcommissuralis; EC—entorhinal cortex; LS—lateral septal nucleus; MFB—medial forebrain bundle; mossy—mossy fibre; MS-DB—medial septal nucleus and nucleus of diagonal band; NC—neocortex; PLC—posterior limbic cortex; PP—perforant path; RF—reticular formation; mR—median raphe nucleus; SC—schaffer collaterals; SUB—subiculum. New powerful reciprocal connections of CA1 with MS added (see *dashed lines*) according to Takacs et al. (2008), as well as well known projections from CA1 to LS according to Risold and Swanson (1996)

625 medial septum (MS) is the central pacemaker and voltage-
 626 controlled oscillator; the CA3 field of the hippocampus is a
 627 comparator or a phase detector; the hippocampal fascia dentata
 628 (FD) is an input mixer and receiver of specific inputs; the
 629 lateral septum (LS) is an output mixer and summator of indi-
 630 vidual lamellas of the CA3 field, i.e. as concurrently operating
 631 sections of the hippocampal formation, almost independent
 632 from each other structurally and functionally (Witter et al.
 633 2000). The similar lamellar structure of the CA1 field and the
 634 corresponding parallel pathways of the limbic system are a
 635 morphological basis for parallel delay-lines. All these struc-
 636 tures, according to Vinogradova (2001) are interconnected and
 637 form two closed loops, as shown in Fig. 9. The first loop deals
 638 with information and includes the hippocampal field CA1,
 639 anterior thalamus, neocortex, and other structures which retain,
 640 even if partially, their signal-specific sensitivity. This loop is
 641 active during initial information memory formation in the
 642 neocortex, as well as during online information treatment,
 643 causing, for example, long delays in the recycling of signals for
 644 the working memory and trace conditioning. The second CA3-
 645 based loop acting as a regulator is responsible for non-specific
 646 brain activation (arousal) and control of the activating reticular
 647 formation. At the same time, the second loop serves as a
 648 negative feedback for regulation of the septal oscillator theta
 649 frequency, with CA3 being a phase detector or comparator. As
 650 a result, the whole ensemble of POs will be synchronized by
 651 phase resetting from CO at the frequency of the system theta
 652 rhythm which is defined by the overall activity of all POs, with
 653 the relative salience of corresponding stimuli taken into
 654 account.

655 The learning rule is non-Hebbian, being based on the
 656 following *Isolability Assumption*: when the number of POs
 657 locked in an ensemble reaches a critical value, their
 658 physiological liabilities⁵ tend to be equalized, i.e. the

oscillators that are gradually brought to a common rhythm 659
 in an ensemble will change their natural frequencies 660
 towards a common one through synthesis of new proteins, 661
 thus implementing isolability coding of information, which 662
 is a form of configural coding. Such learning initially may 663
 be very rapid, (potentially one-shot), while post-learning 664
 fixing of new natural frequencies is rather slow (taking 665
 hours or even days due to consolidation and reconsolida- 666
 tion) and starts after the initial signal retention and some 667
 rest or sleep. The next important assumption is that the 668
 hippocampus functions as a dual comparator system in 669
 which CA3 is the comparator of neocortical and septal 670
 inputs while CA1 is the time comparator of enthorinal 671
 (ECIII) and septal inputs working under inhibition control 672
 from the CA3 field. The outputs of both comparators are 673
 summed in a lateral septum and jointly regulate the theta 674
 frequency of the medial septum: the former for binding of 675
 CS and US representations and the latter for compensation 676
 of long delays between them. 677

678 According to this model, conditioning is a system pro- 679
 cess with many brain structures interacting through theta 680
 synchronization, the septo-hippocampal system being a 681
 global coordinator of various centers. Its operation resets 682
 not only the sustained CA3 activity, like in the model of 683
 Yamazaki and Tanaka (2005) but the whole cortico-septo- 684
 hippocampal system (Kitchigina 2010). The time gap 685
 between CS and US is bridged by means of two mecha- 686
 nisms. The first, in the case of small trace intervals, 687
 involves inherent STM dynamics of cortical columns,

5FL01 ⁵ Liability as temporal unsteadiness in the case of oscillatory networks
 5FL02 can be characterized quantitatively by the value of natural frequency.
 5FL03 The liability is the basic concept of the Russian neurophysiological
 5FL04 school of Vvedensky-Ukhtomsky who maintained that connections
 5FL05 between nervous structures are promoted through the correspondence
 5FL06 in their frequency characteristics that is in equalizing their excitation
 5FL07 cycle rate (Ukhtomsky 1966/1936). Thence follows our Isolability
 5FL08 Assumption.

688 much like the way it appears in the models of Rivest et al.
689 (2009) and Larrauri and Schmajuk (2008). The second
690 mechanism, in the case of long trace intervals, uses the
691 delay line for CS in the CA1-based informational circle,
692 like the tapped delay line of Desmond and Moore (1991).
693 By the same token, the model could also account for a
694 more complex CR, like in the model of Ludvig et al. (2008)
695 and Desmond and Moore (1991). The role of phase tran-
696 sition (arousal acting as the physical temperature param-
697 eter) in this model, like in the model of Rodriguez and Levy
698 (2001), is bridging the time gap in the CA1-based circle.
699 But in contrast to it, the phase transition also provides long
700 controlled delays, by slowing down the dynamics of cortical
701 columns and theta synchronization of all interacting
702 subsystems. Finally, due to similarity of all basic modules
703 with corresponding modules of PAM (pacemaker, accu-
704 mulator, comparator, and memory), this model can be
705 considered as neuronal implementation of PAM (Buhusi
706 and Meck 2005) that can meet all of its challenges.

707 The main predictions that can be derived from the model
708 are as follows. The neocortical columns may act as a per-
709 manent repository of traces in trace conditioning. The medial
710 septum may serve as a global pacemaker and (jointly with
711 septo-hippocampal system) as a ‘core timer’ of variable
712 speed. The hippocampus functioning as a phase comparator
713 (CA3), or as a delay time comparator (CA1), or both, could
714 affect the common septal theta pacemaker to change its
715 frequency in an adaptive way. The CA1-based information
716 circuit can provide the controlled long delays through
717 reverberating the trace of the CS in the limbic system. Due
718 to a circular, or spiral, mode of neural reverberation, the mul-
719 tipleak responses in trace conditioning are possible, most
720 probably, with equidistant intervals between the peaks.
721 Many other behavioral and physiological effects can also be
722 explained with this model; some of them (e.g. habituation,
723 extinction, novelty) were described in the original “Neuro-
724 locator” model of LTM and attention (Kryukov 2008).
725 However, it is not quite clear whether the model is able to
726 strictly generate the scalar property predicted by PAM.
727 Besides, there are some key empirical findings that may be
728 problematic for this model to explain.⁶

- 729 1. Several studies have shown that hippocampal lesions
730 made after training can eliminate trace conditioning.
731 The model’s prediction of an acquisition deficit is clear,
732 but not so is its effect on retrieval or consolidation.
- 733 2. The hippocampus is not related to ISI in trace
734 conditioning in a linear fashion: while in eyeblink
735 conditioning hippocampal involvement emerges at
736 about 500 ms, in fear conditioning it does not occur
737 until 15 or 20 s into the process, which is too long an

interval to support even delay conditioning in eyeblink
(Moyer et al. 1990; Chowdhury et al. 2005). For
example, at 500 ms there is substantial involvement of
the hippocampus in eyeblink but not in trace condi-
tioning. At 3 s no sort of eyeblink conditioning will be
obtained but the hippocampus will not be required for
fear trace conditioning at this interval.

3. There are even data to cast doubt that the hippocampus
has any bridging function in trace conditioning as
similar effects of hippocampal lesions are obtained
when backward trace intervals are used (Quinn et al.
2002). Indeed, it is hard to see that backwards trace
conditioning has anything to do with CR timing. Such
findings are not necessarily fatal problems for this
model. But can they be incorporated in the “unified”
model or do they remain to be serious hurdles?
4. The model is described as non-Hebbian. This may
strike readers as questionable, as NMDA receptors,
which are known to mediate Hebbian plasticity, have
been shown to be critical to trace conditioning (Huerta
et al. 2000; Misane et al. 2005; Quinn et al. 2005).
5. Trace conditioning of eyeblink and fear depend on
different neural substrates downstream from the hippo-
campus (cerebellum and amygdala, respectively). Some-
times the transition between these in the proposed model
is a bit confusing considering that both trace and delay
conditioning depend on the cerebellum, which is not true
of fear, though. This point as well as the above problems
needs to be addressed in greater detail.

Mathematical analysis of the proposed unified model

Nonlinear differential equation of trace conditioning

To answer the above questions we present a short mathe-
matical description of the proposed unified model as a
particular case of the attention and LTM model “Neuro-
locator” which was previously been described by the fol-
lowing system of stochastic integro-differential equations
(Kryukov et al. 1990, Eq. (9.7)).

$$\frac{d\varphi_i}{dt} = \Lambda_{0i} - \left[\sum_{j=1}^n A_{0j} g_j(\varphi_j) + N_j(t) \right] F(p), \quad (i = 1, \dots, n) \quad (1)$$

where φ_i —mean phase difference of the septal and i th
groups of cortical oscillators; Λ_{0i} —frequency detuning
between the cortical and septal oscillators; $A_{0j} g_j(\varphi_j)$ —non-
linear sigmoid output function of the CA3-field phase
comparator in the i th lamella of the hippocampus repre-
senting the cross-correlation of its two major inputs;
 $N_j(t)$ —random walk process of the i th lamella; n —total

6FL01 ⁶ We are grateful to Reviewer #1 for this list of problems.

783 number of lamellas; $F(p)$ —transfer function of the low-
 784 pass mRF filter, which stabilizes the PLL system in case of
 785 e.g. lapse of attention. Operator multiplication by $F(p)$ on
 786 the right-hand side of (1) means convolution with function
 787 $f(t)$, for which $F(p)$ is Laplace transform.

788 In the case of trace conditioning, we first reduce
 789 n-dimensional system (1) to two equations corresponding to
 790 CS and US representation with intensities A_{01} and A_{02}
 791 respectively, but with the same discriminative function $g_3(\varphi)$
 792 of the CA3-based comparator. Then we take into account that,
 793 by the Isolability Assumption and phase reset of POs, Λ_{01}
 794 tends to Λ_{02} , and hence φ_1 stochastically tends to φ_2 , which is
 795 also clear from the numerical simulation of system (1) (Kaz-
 796 anovich et al. 1991, Fig. 5); hence the system (1) with $i = 1, 2$
 797 can be further reduced to the following single equation:

$$\frac{d\varphi}{dt} = \Lambda_0 - [A_t g_3(\varphi) F(p) + N(t)] \quad (2)$$

799 This is a nonlinear integro-differential equation of trace
 800 conditioning sufficient to answer the above questions. Here
 801 $N(t)$ is random walk process with Poissonian jumps and
 802 exponential drift between jumps; its drift rate is equal to $1/T$,
 803 if $F(p) = K/(1 + pT)$, where $K = K_o K_d$ is the loop
 804 gain.⁷ The time-dependent intensity or arousal A_t in Eq. 2
 805 is given by

$$A_t = A_{01} + A_{02} + A_{01}A_{02}g_1(t), \quad (3)$$

807 where the last summand reflects the AND-gate function of
 808 the CA1-field comparator (Vinogradova 2001; Ang et al.
 809 2005). This summand can be explained as follows. If we
 810 assume that $CS(t) = A_{01}1_{CS}(t)$, $US(t) = A_{02}1_{US}(t-ISI)$ and
 811 that the CS-US association can be expressed as cross-
 812 correlation $R_{CS,US}$, then

$$R_{CS,US}(t, \varphi) \int_0^t CS(t-x)US(x)dx = A_{01}A_{02}g_1(t)g_3(\varphi) \quad (4)$$

814 where $g_1(t)$ is the association function of the CA1-field
 815 comparator of CS and US, while the discriminative
 816 function $g_3(\varphi)$ reflects the fact that US arrives at the
 817 input of the CA1-field comparator from the output of the
 818 CA3-field comparator. From (4) we have

$$g_1(t) = \int_0^t 1_{CS}(t-x)1_{US}(x-ISI)dx, \quad (5)$$

820 where $1_{CS}(t) = 1$, if $CS(t) \neq 0$ and $1_{CS}(t) = 0$, otherwise.
 821 The same is true for $1_{US}(t)$. Figure 10 shows the structure
 822 of function $g_1(t)$ for different duration of the CS stimuli.

823 Below, Eqs. 2, 3 and 5 will be used for describing five
 824 basic properties of the proposed unified model along with
 825 the corresponding experimental findings.

826 Boundary conditions for hippocampal involvement
 827 in Pavlovian conditioning

828 Here, we make some additional assumptions which will help
 829 to explain the core mechanism of trace conditioning but will
 830 be dismissed later on. We shall consider Eq. 2 in the deter-
 831 ministic case ($N(t) = 0$), without filter ($F(p) = K$) and with
 832 time-averaged A_t over ISI, i.e.

$$\bar{A}_t = A_{01} + A_{02} + A_{01}A_{02} \frac{\tau_{CS} + \tau_{US}}{ISI}, \quad (6)$$

834 where τ_{CS} and τ_{US} are the durations of CS and US,
 835 respectively. Under such conditions, Eq. 2 takes a simple
 836 form of

$$\frac{d\varphi}{dt} = \Lambda_0 - \bar{A}_t K g_3(\varphi). \quad (7)$$

838 This equation can have a stationary solution only if the
 839 following boundary conditions are fulfilled

$$g_3 \min < \frac{\Lambda_0}{\bar{A}_t K} < g_3 \max, \quad (8)$$

841 which together with Eq. 6 implies that the hippocampus is
 842 involved in trace conditioning only within some interval of
 843 ISI values, in accord with the empirical finding by Misane
 844 et al. (2005). This interval depends on particular values of
 845 $A_{01}A_{02}K/\Lambda_0$: if this value is small it shifts to the lower
 846 values of ISI (e.g. in EBC), if high, it shifts to the higher
 847 values of ISI (e.g. in fear and appetitive conditioning).

848 Moreover, our model predicts that sometimes the hip-
 849 pocampus may be involved in delay conditioning, but not
 850 involved in trace conditioning. To see that let us suppose
 851 that in Eq. 6

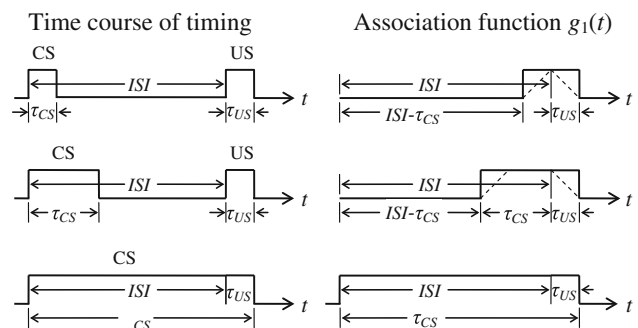
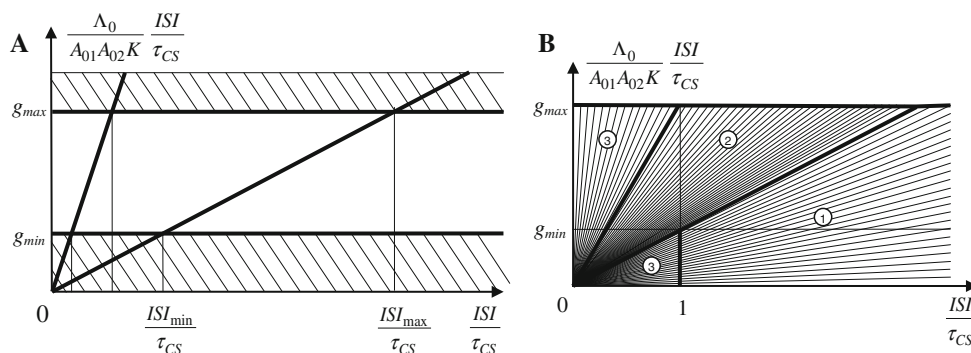


Fig. 10 Association function $g_1(t)$ is formed by time-shifting of CS towards US without overlapping. In fact $g_1(t)$ is not a rectangle but according to Eq. 5 is a triangle for CS and US having equal durations and a trapezium in general case as shown by dashed lines. But since US duration is much less than that of CS, the rectangle is a quite acceptable approximation

7FL01 ⁷ K_o and K_d are transfer coefficients for the septal VCO and the CA3
 7FL02 phase detector, respectively.

Fig. 11 a The upper and lower ISI-boundaries for the hippocampal involvement in the conditioning according to Inequality (10). **b** Three parametric regions of Pavlovian conditioning based on Inequality (10): (1)—“Trace but not delay”; (2)—“Both trace and delay”; (3)—“Delay but not trace”



$$A_{01} + A_{02} \ll A_{01}A_{02}, \quad (9)$$

853 i.e. nonassociative interaction of CS and US is much
854 weaker than that of associative interaction.⁸ Then, instead
855 of (8), we have for $\tau_{CS} \gg \tau_{US}$ approximately

$$g_{3\min} < \frac{\Lambda_0}{A_{01}A_{02}K} \frac{ISI}{\tau_{CS}} < g_{3\max} \quad (10)$$

857 which explicitly expresses the upper and lower ISI bounds
858 for hippocampal involvement in conditioning (see Fig. 11a).
859 From Inequality (10) it follows that the hippocampus may be
860 needed even for delay conditioning ($ISI/\tau_{CS} < 1$) if
861 $A_{01}A_{02}K\tau_{CS}$ is relatively low as found experimentally by
862 Quinn et al. (2008), in case of few training trials or low
863 footshock intensity and Beylin et al. (2001) in case of long
864 delay task. On the contrary, violation of the left side of
865 Inequality (10) means that the hippocampus is not required
866 even in trace conditioning ($ISI/\tau_{CS} > 1$) if ISI is relatively
867 short and/or $A_{01}A_{02}K\tau_{CS}$ is relatively high (as found exper-
868 imentally by Thibaudeau et al. 2007, 2009; Kyd et al. 2008;
869 McGlinchey et al. 2008; Beylin et al. 2001). In general,
870 Eq. 10 provides the boundary lines not only for the hippo-
871 campal involvement in conditioning but also the border lines
872 between trace and conditioning depending on the task diffi-
873 culties (see Fig. 11).

874 Optimal values of trace conditioning parameters

875 Being a system of automatic control, our model has opti-
876 mal processing speed. Therefore, there exists an optimal set
877 of parameters of trace conditioning in which learning is
878 fast. It will occur when e.g. $K = K_0K_d$ is maximal (see
879 footnote 7). Since K_0 is constant, $K_d = dg_3(\varphi)/d\varphi$ should
880 be maximal, which occurs at the point of inflexion $\varphi_0 = \varphi$,
881 such that $d^2g_3(\varphi_0)/(d\varphi)^2 = 0$ (see Fig. 12). In general, not
882 only K_d but each parameter involved in equality $\frac{\Lambda_0}{A_tK} =$
883 $g_3(\varphi_0)$ can be optimal at fixed values of other parameters.

8FL01 ⁸ In fact, the supposition (9) is not true according to Lindquist et al.
8FL02 (2009), but it helps in simple explanation of many so far unexplained
8FL03 experimental findings. .

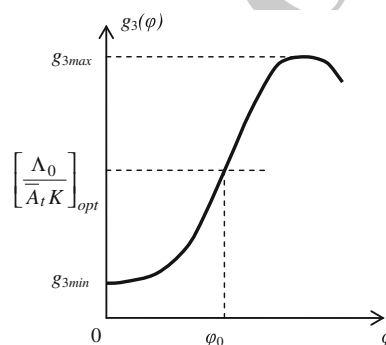


Fig. 12 Non-linear discriminating function of the CA3-field phase comparator

884 However, the shift of any parameter in conditioning from
885 the optimal value will require some additional learning to
886 reach the optimal regime. This optimality property was
887 repeatedly discovered in many experiments. For example,
888 there exist optimal CS duration τ_{CS} (Kehoe et al. 2009),
889 optimal US intensity A_{02} (Oswald et al. 2009), optimal
890 arousal A_t (Berry and Swain 1989; Shors 2001), optimal ISI
891 (Vogel et al. 2004; Kehoe et al. 2010). After the ISI
892 change, additional training proved necessary to allow
893 asymptotic responding at the new ISI (Steinmetz et al.
894 2011).

895 Explanation of timing effects

896 Let us return to the general case, as described by Eq. 2, to
897 make a fundamental assumption relating it to behavior: the
898 conditional response $CR(t)$ can be expressed as a random
899 process that is equal to the positive part of the right hand
900 side of Eq. 2 taken with the opposite sign, i.e.

$$CR(t) = [A_t g_3(\varphi) F(p) + N(t) - \Lambda_0]^+, \quad (11)$$

902 where $[x]^+ = x$, if $x > 0$, and $[x]^+ = 0$, if $x < 0$. Figure 13
903 gives a schematic picture of this assumption when
904 $F(p) = K$. Formation and timing of the CR are as fol-
905 lows: From Eq. 11 it follows that $CR(t) = 0$ at the initial
906 stage of conditioning when A_t is small due to poor

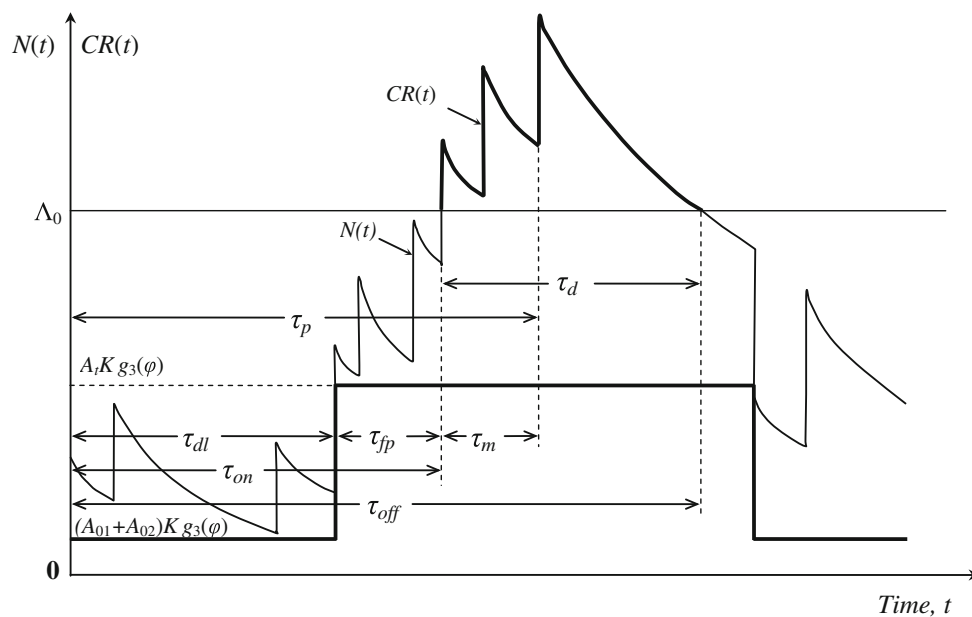


Fig. 13 Schematic representation of the temporal relationship between all the components of $CR(t)$ as defined by Eq. 11 at $F(p) = K$. Note that rectangle in the central part is function $g_1(t)$ multiplied by product $A_{01}A_{02}Kg_3(\varphi)$. It makes most probable crossing of Λ_0 by a random process $N(t)$ near the time at which US occurs. In contrast, the non-associative part of $CR(t)$, connected with earlier portions of the CS is due to crossing of Λ_0 by a process $N(t)$ long before the time at which US appears. It occurs with much lower probability than that of the associative part of $CR(t)$. Pavlov

believed that the earlier portion of the CS developed a conditioned inhibition and called it *inhibition of delay*. Note that the timing of $CR(t)$ is defined by interaction of two major delay sources: the limbic delay time (τ_{dl}) and the first passage time (τ_{fp}) of $N(t)$ through threshold Λ_0 . The other temporal parameters such as peak time (τ_p), duration (τ_d) and the times of CR onset (τ_{on}) and offset (τ_{off}) are only different combinations of these two major delay sources, which allows estimation of variability for each parameter (see Eq. 12) in terms of CVs of these two sources

907 synchronization. Upon repeated stimulation, CS and US
 908 representations become synchronized at a common theta
 909 frequency so that A_r increases causing the time of threshold
 910 Λ_0 being first passed by random process $N(t)$ to be close to
 911 the time of US appearance. With further training this tendency
 912 increases since function A_r , which was initially
 913 evenly distributed over ISI with the mean value given by
 914 (6), becomes concentrated near US due to the function
 915 $g_1(t)$ as it is shown in Fig. 10. From Fig. 13, it can be seen
 916 that acquisition of CR is faster and reaches a higher
 917 asymptote with high $A_r K$, e.g. with more intensive US (in
 918 accord with Oswald et al. 2006), or with more intensive CS
 919 (in accord with Miller et al. 2008; Weinberger 2003; Fritz
 920 et al. 2007; Galvez et al. 2006). Acquisition is complete
 921 when A_r reaches the value at which CR habituates, i.e.
 922 when $\frac{\Lambda_0}{A_r K} < g_{3\min}$, in violation of Inequality (8), and hence
 923 the septo-hippocampal system is switched off. However,
 924 presentation of CS alone (without US) causes dehabitua-
 925 tion⁹ and CR reappears.

926 The above random timing is adaptive in the sense that a
 927 change of any parameter e.g. ISI or CS duration, shifts $\frac{\Lambda_0}{A_r K}$
 928 from the optimal value (shown in Fig. 12), which requires

additional learning (changing $A_{01}A_{02}$) to gain the optimal 929
 regime. In particular, *inhibition of delay* as a constraint on 930
 the CR to a few seconds prior to US delivery, depends on 931
 the ISI duration, such that CR latency decreases when 932
 training is conducted with relatively short ISI but increases 933
 with relatively long ISI, as found experimentally by Vogel 934
 et al. (2003). 935

The most difficult problem of timing is explanation of 936
 its scalar property in terms of neural activity. It requires a 937
 detailed calculation of the mean (M) and the standard 938
 deviation (SD) of the first time of $N(t)$ passage over 939
 threshold Λ_0 . This problem in the context of random walk 940
 models of neuron firing was investigated both analytically 941
 (Kryukov 1976) and by computer simulation (Stein 1967). 942
 In particular, it was found that $CV = SD/M$ varies as 943
 inverse root of the neuronal threshold value, while M is 944
 proportional to the threshold value itself. Thus, the CV can 945
 not be constant and the scalar property can not be explained 946
 in terms of the random walk models. Fortunately, the 947
 latency of CR in the trace conditioning model includes not 948
 only the time of first passage across the threshold Λ_0 but 949
 also the delay in the limbic delay line. Simulation shows 950
 that the latter has a low CV for short delays but a rising 951
 tendency for long delays (see below). Thus, it is possible to 952
 explain a constant CV as a combination of rising and 953

9FL01 ⁹ For the explanation of habituation and dehabituation mechanism
 9FL02 see Kryukov (2008, p. 152).

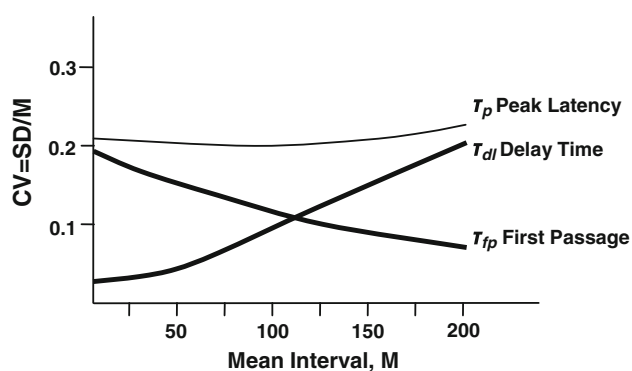


Fig. 14 Constant CV can be at least partially explained as a result of two opposite tendencies

954 declining CVs, at least for not too long delays. To show
955 that, let us calculate the SD of the sum of two independent
956 random delays, one of which has CV with a rising tendency,
957 and the other with a declining tendency.

$$(SD_{\Sigma})^2 = (SD_1)^2 + (SD_2)^2 = (CV_1)^2 M_1^2 + (CV_2)^2 M_2^2,$$

whence

$$(CV_{\Sigma})^2 = (CV_1)^2 \frac{M_1^2}{(M_1 + M_2)^2} + (CV_2)^2 \frac{M_2^2}{(M_1 + M_2)^2}$$

959 In short, CV of the sum of two independent intervals is an
960 almost linear combination of component CVs. Therefore, we
961 can qualitatively estimate the CVs of all random intervals
962 shown in Fig. 13 taking into account both the rising and
963 declining tendencies weighted by their relative duration (see
964 Fig. 14). Comparison of model predictions and experimental
965 CVs presented in Fig. 15 shows that (a) similar timing
966 characteristics have a similar curvilinear dependence on
967 $M \approx ISI$, (b) timing is not strictly scalar across ISI, (c) the
968 only discrepancy is that the model predicts $CV_p > CV_{on}$, i.e.
969 the peak latency is more variable than the onset latency,
970 while in experiment $CV_p < CV_{on}$. A possible reason for this
971 discrepancy may be that $M \neq ISI$, i.e. different abscissas in
972 panels A and B of Fig. 15 are used.

973 The review of timing literature, in accord with the above
974 analyses, shows that the scalar property may be oversimpli-
975 cation of the real data. Contrary to the constant predicted
976 by Weber's law, the Weber fraction (CV) is larger at
977 2 s than at 0.2 s (Lavoie and Grondin 2004). Similarly,
978 Lejeune et al. (2006), showed that the scalar property of
979 variance measured by the CVs of the Gaussian curves
980 would normally hold over a range of durations, but that
981 CVs tended to increase as the interval value became very
982 large. On contrary, Lewis and Miall (2009) found that the
983 CV of human subject timing monotonically decreases.
984 These findings join previous reports in demonstrating a
985 systematic violation of the scalar property in timing data
986 (e.g. Lejeune and Wearden 2006).

Hippocampal lesion effects

987

In general, the effects of hippocampal lesions in trace 988
conditioning are predicted by the Theta-Regulated Attention 989
Theory (Vinogradova 2001) and the "Neurolocator" 990
model (Kryukov 2008), as in the particular case of hippo- 991
campus-dependent memory. But the above specific role of 992
the CA1 and CA3 field as time comparator and phase 993
comparator, respectively, allows predicting the following 994
specific effects. 995

996 Pretraining lesions of CA1 or CA3 or both fields
997 attenuate the acquisition of trace memories. Experimental
998 support for this point can be found in Hunsaker et al.
999 (2009), Kishimoto et al. (2006), Quinn et al. (2005), Bur-
1000 man et al. (2006), Wanisch et al. (2005), Seo et al. (2008),
1001 Yoon and Otto (2007).

1002 Posttraining lesions of the hippocampus result in more
1003 complex effects since the hippocampus is not a place where
1004 the LTM of trace conditioning is stored and there are
1005 several ways in addition to the hippocampus for the
1006 retrieval of memory when the medial septum is activated.
1007 While consolidation, reconsolidation and extinction theo-
1008 retically require an intact hippocampus (Kryukov 2008,
1009 2011a, b) since performance of these tasks is impossible
1010 without phase synchronization, the retrieval/expression is
1011 possible through frequency synchronization, i.e. without
1012 CA3-based regulatory circuits.¹⁰ In such a case, CA1-based
1013 informational circle can alone synchronize CS and US
1014 representations through the direct path to the medial sep-
1015 tum (see dash lines in Fig. 9). Moreover, in the case of both
1016 CA1 and CA3 lesions, the synchronization needed for
1017 retrieval of already consolidated memories can be provided
1018 by the direct path from the mPFC to the medial septum
1019 (Gabbott et al. 2005; Nieuwenhuis and Takashima 2011) or
1020 through phase resetting of theta by the external stimuli
1021 (Sauseng et al. 2008).

1022 The most relevant recent data in support of these pre-
1023 dictions are as follows:

- Lesions restricted to the dorsal hippocampus blocked 1024
acquisition of trace fear conditioning. Larger lesions 1025
were required to impair retrieval of trace fear condi- 1026
tioning (Burman et al. 2006). 1027
- Lesion of CA1 connections with the medial septum 1028
impairs consolidation/retrieval of auditory-cued and 1029
context fear (Hunsaker et al. 2009). 1030
- APV injected in the dorsal hippocampus impairs 1031
acquisition of context memories but does not affect 1032
its retrieval or retrieval of trace fear memories (Matus- 1033
Amat et al. 2007). 1034

¹⁰ For the difference between the phase and the frequency synchro- 10FL01
nization (acquisition) (see Gardner, 1979, Ch. 5). 10FL02

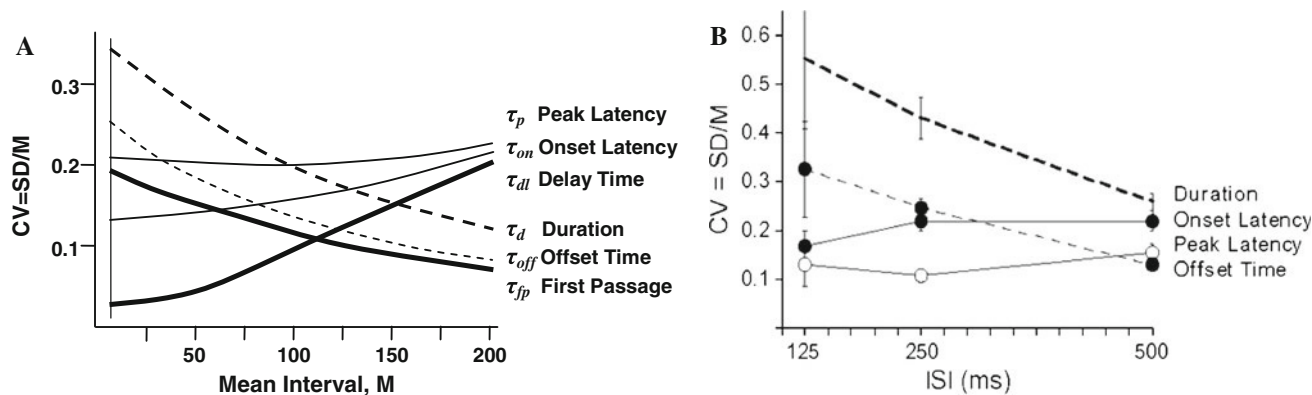


Fig. 15 **a** Model prediction of CVs for each random time interval shown in Fig. 13. The rising CV curve is the same as in the simulation model (see Fig. 16b), the falling CV curve is proportional to $1/\sqrt{M}$, the other curves are plotted according to Eq. 12. **b** Experimental CV

from Kehoe et al. (2010). Note the qualitative agreement of model-predicted curves with experimental ones, except for the unusual upward concavity of the Onset Latency curve, which is probably due to differences in abscissas in **a** and **b** graphs

- 1035 • Retrieval of trace memories is possible without the
1036 hippocampus at short ISI (Chowdhury et al. 2005;
1037 Moyer et al. 1990).
1038 • Trace conditioning is possible without the hippocampus
1039 if CS and US were associated through delay condition-
1040 ing before hippocampal lesion (Beylin et al. 2001).
1041 • Selective lesions in the medial septum induce a
1042 perceptible deficit in acquisition, but not in retrieval
1043 of EBC using the trace paradigm (Fontán-Lozano et al.
1044 2005).

1045 The central role of theta-regulated attention

1046 Since Eq. 2 is only a slight modification of the previously
1047 known equation, governing the attention and the hippo-
1048 campus-dependent memory (Kryukov 2008, Eq. 2), all
1049 properties of attention are applicable to the case of trace
1050 conditioning. For example, the very unusual case of
1051 simultaneous learning of both trace and delay conditioning
1052 with identical ISIs but dissimilar stimuli (Cheng et al.
1053 2008) is only a particular case of divided attention
1054 (Kryukov 2008, p. 150). Another important property of
1055 attention, its transient character, is found in experiments
1056 with the theta-contingent trace conditioning, when learning
1057 is unusually fast during transient computer-defined specific
1058 time intervals of high attention and spontaneous theta
1059 activity (Griffin et al. 2004).

1060 But the most important role of attention in trace condi-
1061 tioning is its mediation in cortical plasticity. Recently, a
1062 new type of memory code was discovered in auditory,
1063 visual and somatosensory cortexes during classical condi-
1064 tioning. Receptive field (RF) plasticity develops in the
1065 primary auditory cortex A1 when a tone CS becomes
1066 associated with an appetitive or aversive US. This associ-
1067 ation is accompanied by shifts of frequency tuning of

neurons toward or to the frequency of the CS. RF plasticity
has all of the major characteristics of behavioral associative
memory: it is highly specific, discriminative, rapidly
induced, consolidating, and can be retained indefinitely
(Weinberger 2003; Edeline 2003). A similar new coding
have been found within the primary visual cortex V1
(Miller et al. 2008), in the extended visual cortex (Bradley
et al. 2003), and in the somatosensory cortex (Galvez et al.
2006). In the latter case, it has also been demonstrated that
during trace EBC learning-related expansion of the cortical
barrel size occurs when rat whisker stimulation is utilized
as a CS and corneal air-puff as a US.

All these data support the general, modality-nonspecific,
theta-contingent learning rule stated in our model as the
Isolability Assumption. According to this assumption, theta
synchronization recruiting new oscillators in common pool
changes the natural frequencies of synchronized oscillators
towards that of the CS oscillators thus rapidly inducing
specific long-term memories. Admittedly, no *direct* evi-
dence has been found yet to this learning rule. Below,
however, we present a series of mutually consistent
attention-dependent effects which add up to count in favor
of the new learning mechanism referred to as the Isolability
Assumption, generalizing the RF cortical plasticity. First, it
is trace rather than delay fear conditioning that requires
attention in mice (Han et al. 2003) and rabbit EBC (Steele-
Russell et al. 2006). Second, attention is the key trigger that
initiates dynamic RF changes and attention-triggered
plasticity in A1 (Fritz et al. 2007). Third, attention is lar-
gely theta-contingent and relies on the hippocampal theta
rhythm. Moreover the theta rhythm is not only a correlate
of attention but is a most important part of the neuronal
mechanism of attention and memory (Vinogradova 2001;
Sauseng et al. 2008; Sirota et al. 2008). Fourth, theta-
contingent training, if it take place only during computer-
defined explicit presence of spontaneous theta activity, has

1104 a dramatic facilitatory effect on trace conditioning: the
 1105 animals given theta-contingent training learned several
 1106 times faster than those given non-theta-contingent training
 1107 (Griffin et al. 2004, Darling et al. 2011), with the number of
 1108 required trials reduced by a factor of up to 4 (Berry and
 1109 Hoffmann 2011; Griffin et al. 2004).

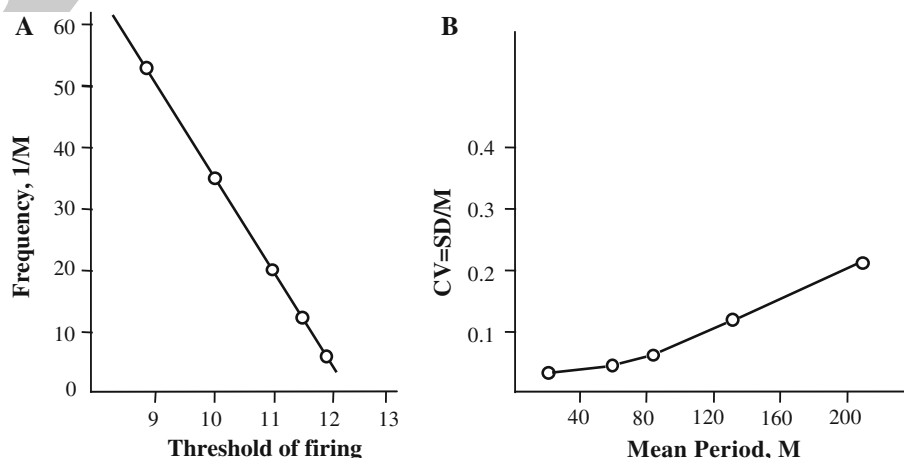
1110 Phase transitions underlie a stimulus trace of long
 1111 duration

1112 The most serious problem of modeling trace conditioning is
 1113 to show how neurons and synapses operating on a millise-
 1114 cond time scale can encode information about time intervals
 1115 on the order of seconds and minutes. Our model solves this
 1116 problem by using the physical phenomenon of critical
 1117 slowdown of neural kinetics near the point of phase transi-
 1118 tion. The existence of phase transitions in physiologically
 1119 plausible neural nets of integrate-and-fire neurons has been
 1120 proved and the lifetimes of long-lived states have been
 1121 estimated (Kryukov et al. 1990), with simulation results
 1122 (Kirillov et al. 1989; Kryukov et al. 1990; Borisyuk and
 1123 Cooke 2007) provided to confirm the theoretical predictions.
 1124 One of the simulation results, which is particularly relevant
 1125 to the problem of long-duration traces, is as follows (see
 1126 Kryukov 2008, Fig. 2). A two-dimensional computer simu-
 1127 lation network of 30×30 integrate-and-fire neurons with
 1128 fixed nearest-neighbor synaptic connections of identical
 1129 strength (Basic Neuronal Model), starts with a spot of units
 1130 of zero background taken as the initial state, and evolves as
 1131 follows. The net activity dwindles to the DOWN state if the
 1132 synaptic strength is small, so that the configuration consist-
 1133 ing mainly of zeros gets stabilized. On the contrary, if the
 1134 synaptic strength is high enough, the spot of units spreads
 1135 out, to result in the UP state. A network with critical
 1136 parameter values, however, is capable of remaining for a
 1137 long time in a state close to the initial one, manifesting itself
 1138 in spot persistence.

This effect is used in formation of a neuronal oscillator
 with the unusual property of very slow oscillations with a
 high period's stability. It is obtained by introducing into the
 above Basic Neuronal Model a single inhibitory neuron
 which receives positive connections of identical strength
 from all neurons, and sends negative connections of iden-
 tical strength to all other neurons. As a result, the network
 becomes capable of producing oscillations of very long
 periods, with small period's variance; a wide range of
 linear frequency regulation is provided by the varying
 threshold of the excitatory neurons. Such oscillators,
 locally connected to each other, can hold the spots of
 activity for a very long time, even after quenching of
 oscillations, which can explain the long-term memory
 traces of previous conditioning. The mathematical theory
 of such persistent states shows (Kryukov et al. 1990,
 p. 250) that their lifetime depends essentially on the
 number of elements in the spot, and can be very long in the
 case of their optimal number, in a way similar to physical
 metastability phenomena. Figure 16 shows the main char-
 acteristics of such a new oscillator: its linearly regulated
 frequency in a wide range and a comparatively low CV of
 oscillation periods.

Unfortunately, this CV is not constant but has an
 upwards tendency over long periods. We supposed that this
 tendency, at least partly, was due to the small size of the
 simulated network. In support of this supposition, we have
 recently reexamined our earlier oscillator simulation results
 (Kirillov et al. 1989) and have found that the supposition to
 be correct. The simulation model is as follows. Tree
 oscillatory submodules A, B, and C are connected con-
 secutively so that submodule A can transmit excitation to
 submodule B, B to C, and C to A, imitating a relay race-
 reverberation in the limbic circle (Batuev 1993). The
 excitation can only be transmitted when the total activity of
 the module reaches its threshold level, i.e. when the cor-
 responding inhibitory neuron fires. After the inhibitory

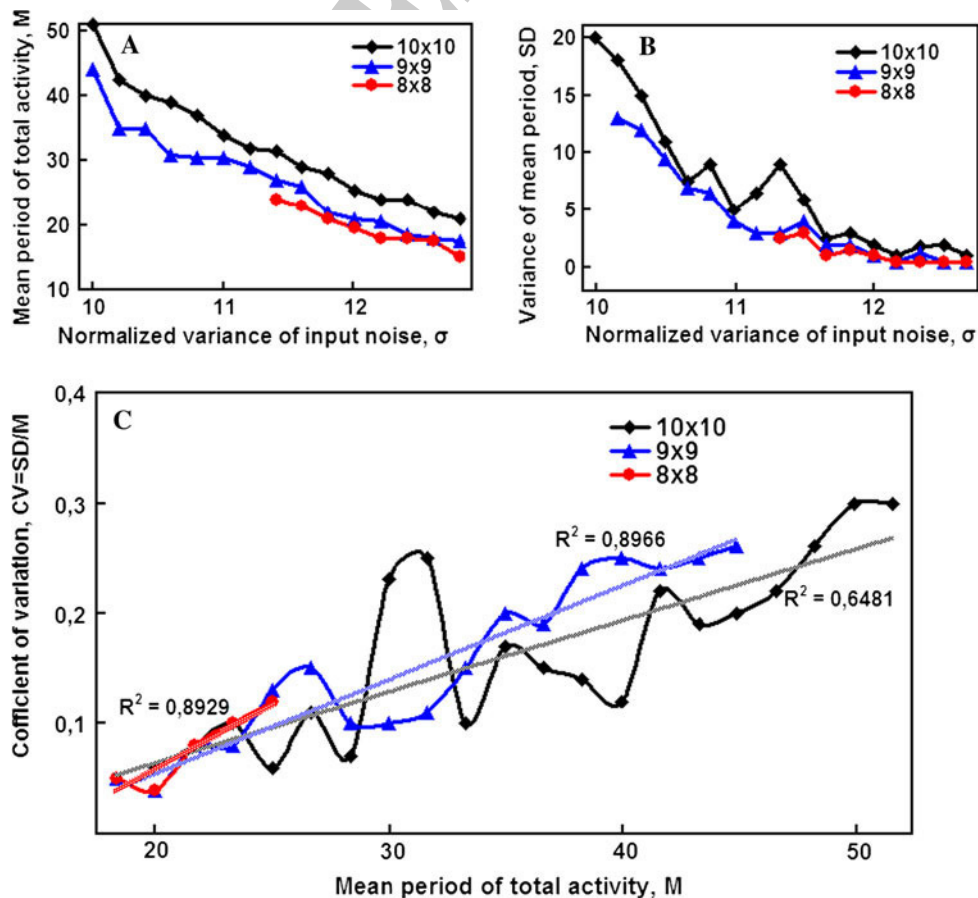
Fig. 16 Two main properties of the simulated "metastable" oscillator: **a** wide range of working frequency and **b** high stability of its period with an upward tendency at long periods



1176 neuron has fired, the activity of its module is set to be small
 1177 enough for the module to be inactive with a high proba-
 1178 bility until excitation from another module comes. There-
 1179 fore, submodules A, B and C work in succession and the
 1180 activity of the whole system is nearly periodic. Figure 17a,
 1181 b display the mean period M and the standard deviation
 1182 (SD) as a function of the noise amplitude σ , representing an
 1183 input control signal. The upper curves in Fig. 17 corre-
 1184 spond to a square 10×10 submodule, the middle ones—to
 1185 a 9×9 submodule and the lower ones—to a 8×8 sub-
 1186 module. Using these simulation results, we have lately
 1187 calculated CV as a function of the mean period M for each
 1188 σ value. The result is presented in Fig. 17c. It shows that
 1189 CV still has the upwards tendency, but this tendency is
 1190 significantly weaker for larger networks. To sum it up, a
 1191 chain of “metastable” oscillators has a fairly stable oscil-
 1192 lation period, its frequency is regulated linearly in a wide
 1193 range, and it can exhibit arbitrarily long oscillation periods
 1194 without changing the time constants of its elements.
 1195 Therefore, it can serve as a neural network model of a
 1196 limbic delay line with long delays. Thus, the solution to the
 1197 problem of long time intervals lies not in a single neuron,
 1198 even less so in its synapses, but in the collective effect
 1199 similar to the one known in statistical physics.

As for its neurobiological substrate, the CA1-based
 information circle with parallel lamellae can operate as a
 parallel delay line. This function is supported by many
 studies on the single neuron level (Vinogradova 2001;
 McEchron et al. 2003; Gilmartin and McEchron 2005), on
 the neural population level (Chen et al. 2009; Batuev
 1993), by the lesion studies (Lee and Kesner 2003; How-
 land et al. 2008; Risterucci et al. 2003; Huerta et al. 2000;
 Misane et al. 2005), by research in the brain imaging
 (Knight et al. 2004), and in the event related potentials
 (Onoda et al. 2003). In particular, a significant number of
 neurons at single and population levels reveal upon
 retrieval maximal firing on CS-alone timed to 10 and 20 s
 after CS, respectively. These latencies were similar to the
 duration of the trace interval used in previous trace condi-
 tioning (McEchron et al. 2003; Chen et al. 2009), which
 means that some sort of timing memory should exist in the
 delay line. As for the longer latencies, the hippocampus
 and the medial prefrontal cortex (mPFC), as critical
 structures of the limbic circle, interact with each other to
 ensure information processing in the time range from 10 s
 up to 5 min (Lee and Kesner 2003) and even up to 30-min
 (Floresco et al. 1997). Such long times periods are proba-
 bly the result of many recurrent NMDAR-dependent

Fig. 17 Simulation results of CA1-based circle. Graphs **a** and **b** are adopted from Kirillov et al. (1989). Graph **c** obtained from graphs **a** and **b** by computing of SD/M for each fixed σ



1224 transmissions in the mPFC-hippocampus loop (Gilmartin
1225 and Helmstetter 2010) with basic recirculation period of
1226 15–30 s (Misane et al. 2005; Huerta et al. 2000).

1227 Discussion

1228 The proposed unified model of trace conditioning is able to
1229 answer the major questions that are currently under dis-
1230 cussion concerning what the hippocampus does during
1231 trace conditioning and how it does it. This model provides
1232 not only a computational mechanism that links several
1233 existing theories for the role of the hippocampus in trace
1234 conditioning, such as gap bridging, overcoming of task
1235 difficulty, and temporal processing; it also identifies the
1236 neurobiological substrate that enable the hippocampus to
1237 perform such a role. For example, the gap bridging is
1238 performed by joint action of both CA1 and CA3 fields, the
1239 former acting as part of the delay line and AND-gate for
1240 restoring CS–US contiguity and the latter as a phase
1241 detector to bind the CS and US representations in the theta
1242 synchronization process as well as to provide US input to
1243 the AND-gate. Such a way of restoring the contiguity is
1244 independent of which of the two stimuli comes first,
1245 because Eq. 6 is symmetric with respect to the CS and US
1246 action, although the time to reach the asymptote depends
1247 strongly on their time order, wherefore the backward trace
1248 conditioning is much slower to learn than the usual forward
1249 one.¹¹

1250 Another important question is how the proposed unified
1251 model could explain the key empirical finding that a
1252 boundary between trace and delay conditioning has 40-fold
1253 difference in the ISI for the fear and eyeblink conditioning
1254 (Chowdhury et al. 2005). The proposed unified model give
1255 an unexpected answer: there is no clear-cut ISI-defined
1256 boundary between the two paradigms, since their respec-
1257 tive task difficulties depend not only on the ISI value but
1258 also on the whole set of conditioning parameters which for
1259 the hippocampus to be involved must meet the strict
1260 mathematical limitation expressed, e.g. by Eq. 10. On the
1261 contrary, the ISI or trace interval values alone as indicators
1262 of the hippocampal involvement may prove misleading
1263 unless the CS duration and other parameters are given. For
1264 example, Chowdhury et al. (2005) and Burman and Gew-
1265 irtz (2007) for a similar task using the same (3-s) trace
1266 interval, obtained seemingly contradictory results because
1267 they used very different CS durations.

1268 But how does the hippocampus “know” which task is
1269 difficult enough to be involved in it or what information must

1270 be processed and maintained for establishing a hippocam-
1271 pus-dependent trace memory versus that for the delay-type
1272 memory (Shors 2004)? The answer is unexpectedly simple:
1273 it (hippocampus) does not “know” that and starts the same
1274 operations regardless of the paradigm, but an easier delay
1275 conditioning task will produce earlier habituation to stimuli
1276 and the hippocampus will switch off at very early stages of
1277 delay conditioning. This explains why delay conditioning is
1278 frequently considered as procedural and hippocampus-
1279 independent memory, while trace conditioning is treated as
1280 declarative, hippocampus-dependent memory requiring
1281 conscious expectance (awareness) for when US is going to
1282 occur. In fact, evidence was found for a dissociation of CRs
1283 and US expectance occurring regardless of whether there
1284 was a delay or trace conditioning (Weidemann et al. 2011).
1285 Similarly, adult neurogenesis in hippocampus FD can not be
1286 considered longer as required for trace, but not delay, con-
1287 ditioning, since mice, specifically, lacking adult neurogen-
1288 esis showed proper fear conditioning and many other
1289 hippocampus-dependent functions (Jaholkowski et al.
1290 2009).

1291 The learning rule of the proposed unified model is non-
1292 Hebbian because according to the Isolability Assumption, a
1293 basic element of learning is not a synapse, nor even a whole
1294 neuron, but a small oscillatory neural network capable of
1295 changing its natural frequency as a result of collective syn-
1296 chronization of isolabile oscillators during learning. The new
1297 learning rule can explain many memory effects that are
1298 problematic for Hebbian learning, such as reconsolidation,
1299 extinction, backward conditioning, etc. A question arises as
1300 to how this new learning rule can match the data on the
1301 critical role of NMDARs in trace but not delay conditioning
1302 (Seo et al. 2008; Gilmartin and Helmstetter 2010; Wanisch
1303 et al. 2005). A key to this question can be found in the paper
1304 of Clafin et al. (2005) which suggests that trace and delay
1305 conditioning have different neural mechanisms for timing
1306 but a common neural substrate for memory acquisition. We
1307 assume that this different mechanism is NMDARs-depend-
1308 ent transmission in the limbic delay line, which is consistent
1309 with the available data (Huerta et al. 2000; Gilmartin and
1310 Helmstetter 2010; Sakamoto et al. 2005; Gruart et al. 2006,
1311 Misane et al. 2005), while the common neural substrate for
1312 trace and delay learning is mainly the sensory cortical theta-
1313 dependent plasticity according to the Isolability Assumption.
1314 Both the temporal and sensory mechanisms are interdepend-
1315 ent in that the delay line needs sensory synchronization of
1316 CS and US representations to restore the CS–US contiguity
1317 in the CA1 AND-gate, while cortical sensory memory
1318 depends on timing of US, in accord with Miller et al. (2008),
1319 Galvez et al. (2006, 2007), and Shuler and Bear (2006).

1320 The critical role of NMDARs in trace conditioning does
1321 not mean that a trace conditioning model should be based on
1322 Hebbian learning for the only reason that NMDARs is also

11FL01 ¹¹ Formally our model explains this asymmetry in learning by less
11FL02 favorable initial state for Eq. 7 to reach the stationary state if US
11FL03 comes before CS.

1323 known to mediate the Hebbian LTP. Firstly, trace condi-
 1324 tioning is a comparatively slow process requiring a large
 1325 number of paired CS–US presentations and therefore cannot
 1326 be directly related to the rapid LTP mechanism (Gruart et al.
 1327 2006). Secondly, there exists non-Hebbian LTP (Kato et al.
 1328 2009; Engert and Bonhoeffer 1997; Tsukamoto et al. 2003).
 1329 Thirdly, the Hebbian LTP is computationally insufficient for
 1330 simulation of many real conditioning features (Krasne et al.
 1331 2011). Nevertheless, the memory mechanism in the pro-
 1332 posed unified model can be considered as a functional analog
 1333 or, rather, as generalization of the Hebbian LTP since both
 1334 mechanisms (a) have the property of associability of weak
 1335 input with delayed strong stimulus, (b) require synchronous
 1336 activation of two or more functional units, neurons and
 1337 neuronal oscillators, respectively, (c) depend upon the syn-
 1338 thesis of new proteins, and (d) are most effectively induced
 1339 by the theta frequency stimulation. However, unlike Hebbian
 1340 LTP, the learning mechanism in the proposed unified model
 1341 provides life-long bidirectional association of two (or more)
 1342 stimuli regardless of the distance between the location of
 1343 their representations in the brain, and, most importantly,
 1344 have no problems with the information shifting from the
 1345 hippocampus to the cortex which arise in the contemporary
 1346 consolidation theory (Frey and Morris 1997; Lesburguères
 1347 et al. 2011).

1348 The important question about the functions of different
 1349 brain structures, such amygdale and cerebellum, in trace
 1350 conditioning can not be adequately discussed here since
 1351 Eq. 1, which can describe their role, is reduced here to
 1352 single Eq. 2. Nevertheless, it is quite clear that the PLL
 1353 system, being a global synchronization system, makes less
 1354 than probable the existence of separate specialized memory
 1355 systems for different paradigms, and even less so for dif-
 1356 ferent types of trace conditioning. For example, fear and
 1357 EBC are universally considered as dependent on different
 1358 neural substrates downstream from the hippocampus (am-
 1359 ygdale and cerebellum, respectively), but according to the
 1360 model architecture shown in Fig. 7, they both take part in
 1361 fear and EBC as partner POs. This unusual prediction of
 1362 our model was recently confirmed by Timmann et al.
 1363 (2010) who showed that the cerebellum was involved in
 1364 motor, emotional and cognitive associative learning using
 1365 classical eyeblink and fear conditioning.

1366 Conclusions

1367 This short review of trace conditioning models shows that
 1368 there exists a computational potential for building a unified
 1369 model but simultaneously points to the serious difficulties
 1370 yet to be overcome. The first point leads to two objectives:
 1371 (a) to fill the time gap by means of a delay line appended
 1372 by phase transition to lengthen the delay duration and (b) to

1373 use a new model architecture similar to that of PAM but
 1374 with a global pacemaker automatically regulated by the
 1375 septo-hippocampal loop to incorporate the attention in
 1376 conditioning. The second more difficult aspect of modeling
 1377 may be reduced to three major problems:

1. A way (if any) to be found to relate the unified model
 1378 to the prevailing memory system theory which requires
 1379 different neuronal substrates for declarative, proce-
 1380 dural, and emotional memories and a different role of
 1381 the hippocampus therein. 1382
2. The unified model should explain how neurons and
 1383 synapses operating on a millisecond time scale can
 1384 encode information about trace intervals on the order
 1385 of seconds and tens of seconds. 1386
3. The learning algorithm of the unified model should be
 1387 able LTM of trace conditioning reconcile to the short
 1388 living hippocampal LTP. 1389

1390 By combining the desired features of existing models
 1391 the proposed unified model of trace conditioning, provides
 1392 a solution to the above three major problems and as a result
 1393 is capable of explaining most of the experimental effects in
 1394 the field. Therefore, this model is the best candidate for a
 1395 unified model of trace conditioning. 1395

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